

Code No: R1641033

R16

Set No. 1

IV B.Tech I Semester Regular/Supplementary Examinations, Jan/Feb - 2022

FINITE ELEMENT METHODS

(Common to Mechanical Engineering and Automobile Engineering)

Time: 3 hours

Max. Marks: 70

Question paper consists of Part-A and Part-B

Answer ALL sub questions from Part-A

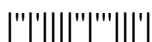
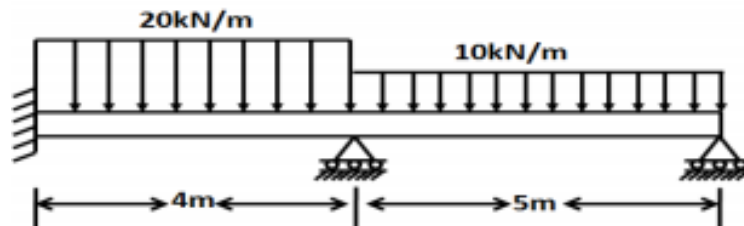
Answer any FOUR questions from Part-B

PART-A (14 Marks)

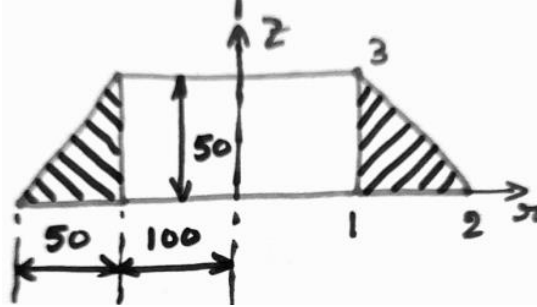
1. a) Write the advantages of finite element methods. [3]
- b) What is band width of a matrix? [2]
- c) Derive an element stress equation for a truss element. [2]
- d) Write the [D] matrix for an axisymmetric body. [3]
- e) What are isoparametric elements? [2]
- f) What is an eigen vector? [2]

PART-B (4x14 = 56 Marks)

2. a) Discuss about Galerkin weighted residual method. [5]
- b) Derive an expression for element stiffness matrix for 2-noded 1-D element using potential energy approach. [9]
3. a) Explain the factors to be considered in selecting interpolation function [5]
- b) Differentiate between the natural and essential boundary conditions. [4]
- c) Discuss about band width and node numbering [5]
4. For the beam shown in Figure, compute slope at the hinged support points. Take $E=200\text{GPa}$, $I=4 \times 10^{-6} \text{ m}^4$. Use two beam elements. [14]



5. a) An axisymmetric ring (triangular element) is shown in the figure. Derive the [B] and [D] matrices. Take $E = 20 \times 10^4 \text{ N/mm}^2$ and $\nu = 0.33$ [10]



- b) Derive the shape functions of CST element. [4]
6. a) Determine the shape functions for a quadrilateral isoparametric element. [6]
 b) Evaluate the following integral using one point and two point gaussian quadrature formulae and compare the results with exact solution.

$$\int_{-1}^1 (2x^3 + 5x^2 + 6) dx$$
 [5]
 c) Derive the shape functions of 1D quadratic element. [3]
7. a) Find the temperature distribution in 1D rectangular cross section fin with 8 cm long, 4 cm wide, 1 cm thick. Assume that convective heat loss occurs from the end of the fin. Take $K = 3 \text{ W/cm-K}$, $h = 0.1 \text{ W/cm}^2\text{-K}$ and $T_a = 20^\circ\text{C}$. Tip temperature is 100°C . [8]
 b) Derive the consistent mass matrix of 2 node beam element [6]

