

BOARD OF INTERMEDIATE EDUCATION
JUNIOR INTER MATHEMATICS PAPER – 1 (A)
MODEL PAPER (ENGLISH VERSION)

TIME: 3 HOURS

MAX.MARKS: 75

SECTION – A

I. i) Very Short Answer Type questions.

ii) Answer ALL questions.

iii) Each question carries TWO marks.

10 × 2 = 20

1. Find the domain of the real valued function $f(x) = \sqrt{2-x} + \sqrt{1+x}$

2. If $f = \{(1, 2), (2, -3), (3, -1)\}$ then find i) $2f$ ii) \sqrt{f} .

3. If $A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 3 & 4 \\ 5 & -6 & x \end{pmatrix}$ and $\det A = 45$ then find 'x'.

4. Find the adjoint and the inverse of the matrix $\begin{bmatrix} \cos \alpha & \sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$

5. If the vectors $-3\bar{i} + 4\bar{j} + \lambda\bar{k}$ and $\mu\bar{i} + 8\bar{j} + 6\bar{k}$ are collinear vectors then find 'λ' and 'μ'.

6. Find the vector equation of the plane passing through the point (0, 0, 0), (0, 5, 0) and (2, 0, 1).

7. Find the area of the parallelogram having $2\bar{i} - 3\bar{j}$ and $3\bar{i} - \bar{k}$ are adjacent sides.

8. Find the period of the function $f(x) = \tan(x + 4x + 9x + \dots + n^2x)$ (n is +ve integer).

9. If $\cos A = \sqrt{\frac{\sqrt{2}+1}{2\sqrt{2}}}$, find the value of $\cos 2A$.

10. For any $x \in \mathbb{R}$ prove that $\cos h^4 x - \sin h^4 x = \cos h(2x)$.

SECTION – B

II. i) Short Answer Type questions.

ii) Answer any FIVE questions.

iii) Each question carries FOUR marks.

5 × 4 = 20

11. Find the value of x, if $\begin{vmatrix} x-2 & 2x-3 & 3x-4 \\ x-4 & 2x-9 & 3x-16 \\ x-8 & 2x-27 & 3x-64 \end{vmatrix} = 0$.

12. If the points whose position vectors are $3\bar{i} - 2\bar{j} - \bar{k}$, $2\bar{i} + 3\bar{j} - 4\bar{k}$, $-\bar{i} + \bar{j} + 2\bar{k}$ and $4\bar{i} + 5\bar{j} + \lambda\bar{k}$ are coplanar, then show that $\lambda = \frac{-146}{17}$.

13. Find the unit vector perpendicular to the plane passing through the points (1, 2, 3), (2, -1, 1) and (1, 2, -4).

14. Prove that $\sin \frac{\pi}{5} \sin \frac{2\pi}{5} \sin \frac{3\pi}{5} \sin \frac{4\pi}{5} = \frac{5}{16}$.
15. If θ_1, θ_2 are solutions of the equation $a \cos 2\theta + b \sin 2\theta = c$, $\tan \theta_1 \neq \tan \theta_2$ and $a + c \neq 0$, then find the value of
 i) $\tan \theta_1 + \tan \theta_2$ ii) $\tan \theta_1 \cdot \tan \theta_2$
16. Prove that $\sin^{-1} \left(\frac{4}{5} \right) + \sin^{-1} \left(\frac{7}{25} \right) = \sin^{-1} \left(\frac{117}{125} \right)$.
17. $\cot A + \cot B + \cot C = \frac{a^2 + b^2 + c^2}{4\Delta}$

SECTION - C

III. i) Long Answer Type questions.

ii) Answer any FIVE questions.

iii) Each question carries SEVEN marks.

5 × 7 = 35

18. Let $f : A \rightarrow B$ be a bijection. Then show that $f \circ f^{-1} = I_B$ and $f^{-1} \circ f = I_A$
19. Show that $3 \cdot 5^{2n+1} + 2^{3n+1}$ is divisible by 17, $\forall n \in \mathbb{N}$.
20. If $\begin{vmatrix} a & a^2 & 1+a^3 \\ b & b^2 & 1+b^3 \\ c & c^2 & 1+c^3 \end{vmatrix} = 0$ and $\begin{vmatrix} a & a^2 & 1 \\ b & b^2 & 1 \\ c & c^2 & 1 \end{vmatrix} \neq 0$, then show that $abc = -1$.
21. Solve the following simultaneous linear equation by using Cramer's rule $2x - y + 3z = 9$, $x + y + z = 6$, $x - y + z = 2$.
22. Show that in any triangle the altitudes are concurrent.
23. If $A + B + C = 180^\circ$, then prove that $\cos^2 \frac{A}{2} + \cos^2 \frac{B}{2} + \cos^2 \frac{C}{2} = 2 \left(1 + \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2} \right)$
24. If $a = 13$, $b = 14$, $c = 15$, show that $R = \frac{65}{8}$, $r = 4$, $r_1 = \frac{21}{2}$, $r_2 = 12$ and $r_3 = 14$